

Linear Equations in Two VariablesExercise 4.1 Page: 68

1. The cost of a notebook is twice the cost of a pen. Write a linear equation in two variables to represent this statement.

(Take the cost of a notebook to be ₹ x and that of a pen to be ₹ y)

Solution:

Let the cost of a notebook be = ₹ x

Let the cost of a pen be = ₹ y

According to the question,

The cost of a notebook is twice the cost of a pen.

i.e., cost of a notebook = $2 \times$ cost of a pen

$$x = 2 \times y$$

$$x = 2y$$

$$x - 2y = 0$$

$x - 2y = 0$ is the linear equation in two variables to represent the statement, 'The cost of a notebook is twice the cost of a pen.'

2. Express the following linear equations in the form $ax + by + c = 0$ and indicate the values of a, b and c in each case.

(i) $2x + 3y = 9.35$

Solution:

$$2x + 3y = 9.35$$

Re-arranging the equation, we get,

$$2x + 3y - 9.35 = 0$$

The equation $2x + 3y - 9.35 = 0$ can be written as,

$$2x + 3y + (-9.35) = 0$$

Now comparing $2x + 3y + (-9.35) = 0$ with $ax + by + c = 0$

We get,

$$a = 2$$

$$b = 3$$

$$c = -9.35$$

(ii) $x - (y/5) - 10 = 0$

Solution:

The equation $x - (y/5) - 10 = 0$ can be written as,

$$1x + (-1/5)y + (-10) = 0$$

Now comparing $x + (-1/5)y + (-10) = 0$ with $ax + by + c = 0$

We get,

$$a = 1$$

$$b = -(1/5)$$

$$c = -10$$

$$(iii) -2x+3y = 6$$

Solution:

$$-2x+3y = 6$$

Re-arranging the equation, we get,

$$-2x+3y-6 = 0$$

The equation $-2x+3y-6 = 0$ can be written as,

$$(-2)x+3y+(-6) = 0$$

Now, comparing $(-2)x+3y+(-6) = 0$ with $ax+by+c = 0$

We get, $a = -2$

$$b = 3$$

$$c = -6$$

$$(iv) x = 3y$$

Solution:

$$x = 3y$$

Re-arranging the equation, we get,

$$x-3y = 0$$

The equation $x-3y=0$ can be written as,

$$1x+(-3)y+(0)c = 0$$

Now comparing $1x+(-3)y+(0)c = 0$ with $ax+by+c = 0$

We get $a = 1$

$$b = -3$$

$$c = 0$$

$$(v) 2x = -5y$$

Solution:

$$2x = -5y$$

Re-arranging the equation, we get,

$$2x+5y = 0$$

The equation $2x+5y = 0$ can be written as,

$$2x+5y+0 = 0$$

Now, comparing $2x+5y+0 = 0$ with $ax+by+c = 0$

We get $a = 2$

$$b = 5$$

$$c = 0$$

(vi) $3x+2 = 0$

Solution:

$3x+2 = 0$

The equation $3x+2 = 0$ can be written as,

$3x+0y+2 = 0$

Now comparing $3x+0+2 = 0$ with $ax+by+c = 0$ We get $a = 3$

$b = 0$

$c = 2$

(vii) $y-2 = 0$

Solution:

$y-2 = 0$

The equation $y-2 = 0$ can be written as,

$0x+1y+(-2) = 0$

Now comparing $0x+1y+(-2) = 0$ with $ax+by+c = 0$ We get $a = 0$

$b = 1$

$c = -2$

(viii) $5 = 2x$

Solution:

$5 = 2x$

Re-arranging the equation, we get,

$2x = 5$

i.e., $2x-5 = 0$

The equation $2x-5 = 0$ can be written as,

$2x+0y-5 = 0$

Now comparing $2x+0y-5 = 0$ with $ax+by+c = 0$ We get $a = 2$

$b = 0$

$c = -5$

Exercise 4.2 Page: 70**1. Which one of the following options is true, and why?** **$y = 3x+5$ has**

1. A unique solution
2. Only two solutions
3. Infinitely many solutions

Solution:

Let us substitute different values for x in the linear equation $y = 3x + 5$

x	0	1	2	100
y, where $y = 3x + 5$	5	8	11	305

From the table, it is clear that x can have infinite values, and for all the infinite values of x, there are infinite values of y as well.

Hence, (iii) infinitely many solutions is the only option true.

2. Write four solutions for each of the following equations:

(i) $2x + y = 7$

Solution:

To find the four solutions of $2x + y = 7$, we substitute different values for x and y.

Let $x = 0$

Then,

$$2x + y = 7$$

$$(2 \times 0) + y = 7$$

$$y = 7$$

(0,7)

Let $x = 1$

Then,

$$2x + y = 7$$

$$(2 \times 1) + y = 7$$

$$2 + y = 7$$

$$y = 7 - 2$$

$$y = 5$$

(1,5)

Let $y = 1$

Then,

$$2x + y = 7$$

$$(2x) + 1 = 7$$

$$2x = 7 - 1$$

$$2x = 6$$

$$x = 6/2$$

$$x = 3$$

(3,1)

Let $x = 2$

Then,

$$2x + y = 7$$

$$(2 \times 2) + y = 7$$

$$4 + y = 7$$

$$y = 7 - 4$$

$$y = 3$$

$$(2, 3)$$

The solutions are $(0, 7), (1, 5), (3, 1), (2, 3)$

(ii) $\pi x + y = 9$

Solution:

To find the four solutions of $\pi x + y = 9$, we substitute different values for x and y .

Let $x = 0$

Then,

$$\pi x + y = 9$$

$$(\pi \times 0) + y = 9$$

$$y = 9$$

$$(0, 9)$$

Let $x = 1$

Then,

$$\pi x + y = 9$$

$$(\pi \times 1) + y = 9$$

$$\pi + y = 9$$

$$y = 9 - \pi$$

$$(1, 9 - \pi)$$

Let $y = 0$

Then,

$$\pi x + y = 9$$

$$\pi x + 0 = 9$$

$$\pi x = 9$$

$$x = 9/\pi$$

$$(9/\pi, 0)$$

Let $x = -1$

Then,

$$\pi x + y = 9$$

$$(\pi \times -1) + y = 9$$

$$-\pi + y = 9$$

$$y = 9 + \pi$$

$$(-1, 9 + \pi)$$

The solutions are $(0, 9)$, $(1, 9 - \pi)$, $(9/\pi, 0)$, $(-1, 9 + \pi)$

(iii) $x = 4y$

Solution:

To find the four solutions of $x = 4y$, we substitute different values for x and y .

Let $x = 0$

Then,

$$x = 4y$$

$$0 = 4y$$

$$4y = 0$$

$$y = 0/4$$

$$y = 0$$

$$(0, 0)$$

Let $x = 1$

Then,

$$x = 4y$$

$$1 = 4y$$

$$4y = 1$$

$$y = 1/4$$

$$(1, 1/4)$$

Let $y = 4$

Then,

$$x = 4y$$

$$x = 4 \times 4$$

$$x = 16$$

$$(16, 4)$$

Let $y = 1$

Then,

$$x = 4y$$

$$x = 4 \times 1$$

$$x = 4$$

$$(4, 1)$$

The solutions are $(0, 0)$, $(1, 1/4)$, $(16, 4)$, $(4, 1)$

3. Check which of the following are solutions of the equation $x-2y = 4$ and which are not:

(i) (0, 2)

(ii) (2, 0)

(iii) (4, 0)

(iv) ($\sqrt{2}$, $4\sqrt{2}$)

(v) (1, 1)

Solutions:

(i) (0, 2)

$(x,y) = (0,2)$

Here, $x=0$ and $y=2$

Substituting the values of x and y in the equation $x-2y = 4$, we get,

$$x-2y = 4$$

$$\Rightarrow 0 - (2 \times 2) = 4$$

But, $-4 \neq 4$

$(0, 2)$ is **not** a solution of the equation $x-2y = 4$

(ii) (2, 0)

$(x,y) = (2, 0)$

Here, $x = 2$ and $y = 0$

Substituting the values of x and y in the equation $x-2y = 4$, we get,

$$x-2y = 4$$

$$\Rightarrow 2 - (2 \times 0) = 4$$

$$\Rightarrow 2 - 0 = 4$$

But, $2 \neq 4$

$(2, 0)$ is **not** a solution of the equation $x-2y = 4$

(iii) (4, 0)

Solution:

$(x,y) = (4, 0)$

Here, $x= 4$ and $y=0$

Substituting the values of x and y in the equation $x-2y = 4$, we get,

$$x-2y = 4$$

$$\Rightarrow 4 - 2 \times 0 = 4$$

$$\Rightarrow 4 - 0 = 4$$

$$\Rightarrow 4 = 4$$

$(4, 0)$ is a solution of the equation $x-2y = 4$

(iv) ($\sqrt{2}$, $4\sqrt{2}$)

Solution:

$$(x,y) = (\sqrt{2}, 4\sqrt{2})$$

Here, $x = \sqrt{2}$ and $y = 4\sqrt{2}$

Substituting the values of x and y in the equation $x-2y = 4$, we get,

$$x - 2y = 4$$

$$\Rightarrow \sqrt{2} - (2 \times 4\sqrt{2}) = 4$$

$$\sqrt{2} - 8\sqrt{2} = 4$$

But, $-7\sqrt{2} \neq 4$

$(\sqrt{2}, 4\sqrt{2})$ is **not** a solution of the equation $x-2y = 4$

(v) (1, 1)

Solution:

$$(x,y) = (1, 1)$$

Here, $x = 1$ and $y = 1$

Substituting the values of x and y in the equation $x-2y = 4$, we get,

$$x - 2y = 4$$

$$\Rightarrow 1 - (2 \times 1) = 4$$

$$\Rightarrow 1 - 2 = 4$$

But, $-1 \neq 4$

$(1, 1)$ is **not** a solution of the equation $x-2y = 4$

4. Find the value of k , if $x = 2$, $y = 1$ is a solution of the equation $2x+3y = k$.

Solution:

The given equation is

$$2x+3y = k$$

According to the question, $x = 2$ and $y = 1$

Now, substituting the values of x and y in the equation $2x+3y = k$,

We get,

$$(2 \times 2) + (3 \times 1) = k$$

$$\Rightarrow 4 + 3 = k$$

$$\Rightarrow 7 = k$$

$$k = 7$$

The value of k , if $x = 2$, $y = 1$ is a solution of the equation $2x+3y = k$, is 7.

Exercise 4.3 Page: 74

1. Draw the graph of each of the following linear equations in two variables:

(i) $x+y = 4$

Solution:

To draw a graph of linear equations in two variables, let us find out the points to plot.

LOYAL EDUCATION MATHEMATICS

Result Oriented

(NCERT SOLUTION)

[CLASS IX]

To find out the points, we have to find the values which x and y can have, satisfying the equation.

Here,

$$x+y = 4$$

Substituting the values for x ,

$$\text{When } x = 0,$$

$$x+y = 4$$

$$0+y = 4$$

$$y = 4$$

$$\text{When } x = 4,$$

$$x+y = 4$$

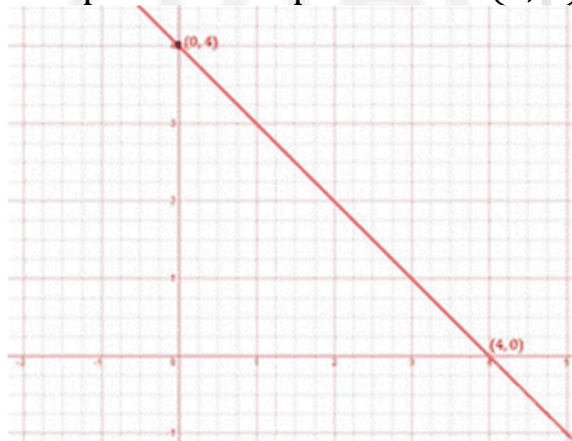
$$4+y = 4$$

$$y = 4-4$$

$$y = 0$$

x	y
0	4
4	0

The points to be plotted are $(0, 4)$ and $(4, 0)$



(ii) $x-y = 2$

Solution:

To draw a graph of linear equations in two variables, let us find out the points to plot.

To find out the points, we have to find the values which x and y can have, satisfying the equation.

Here,

$$x - y = 2$$

Substituting the values for x,

$$\text{When } x = 0,$$

$$x - y = 2$$

$$0 - y = 2$$

$$y = -2$$

$$\text{When } x = 2,$$

$$x - y = 2$$

$$2 - y = 2$$

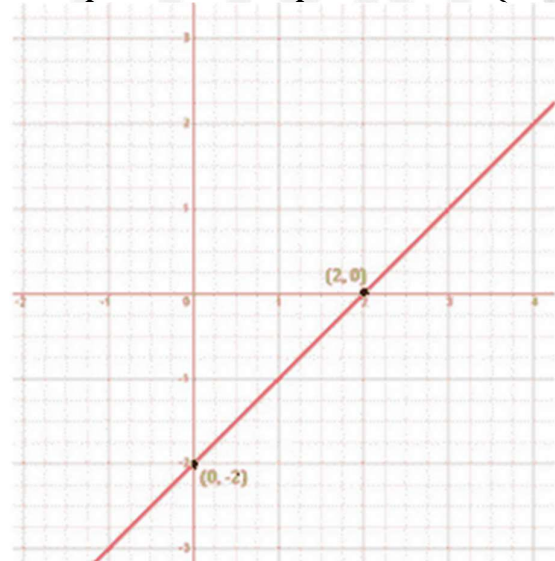
$$-y = 2 - 2$$

$$-y = 0$$

$$y = 0$$

x	y
0	-2
2	0

The points to be plotted are (0, -2) and (2, 0)



(iii) $y = 3x$

Solution:

To draw a graph of linear equations in two variables, let us find out the points to plot.

LOYAL EDUCATION MATHEMATICS

Result Oriented

(NCERT SOLUTION)

[CLASS IX]

To find out the points, we have to find the values which x and y can have, satisfying the equation.

Here,

$$y = 3x$$

Substituting the values for x,

When $x = 0$,

$$y = 3x$$

$$y = 3 \times 0$$

$$y = 0$$

When $x = 1$,

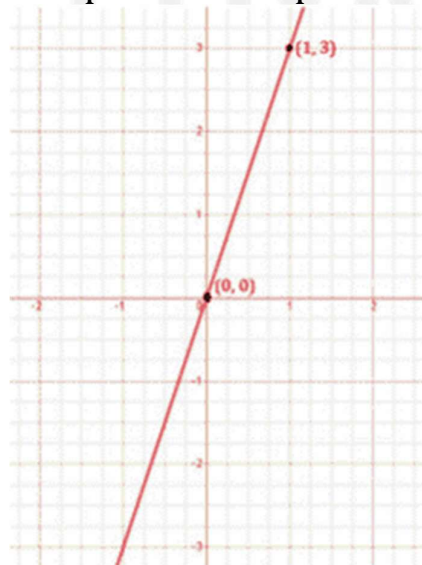
$$y = 3x$$

$$y = 3 \times 1$$

$$y = 3$$

x	y
0	0
1	3

The points to be plotted are (0, 0) and (1, 3)



(iv) $3 = 2x + y$

Solution:

To draw a graph of linear equations in two variables, let us find out the points to plot.

LOYAL EDUCATION MATHEMATICS

Result Oriented

(NCERT SOLUTION)

[CLASS IX]

To find out the points, we have to find the values which x and y can have, satisfying the equation.

Here,

$$3 = 2x + y$$

Substituting the values for x,

$$\text{When } x = 0,$$

$$3 = 2x + y$$

$$3 = 2 \times 0 + y$$

$$3 = 0 + y$$

$$y = 3$$

$$\text{When } x = 1,$$

$$3 = 2x + y$$

$$3 = 2 \times 1 + y$$

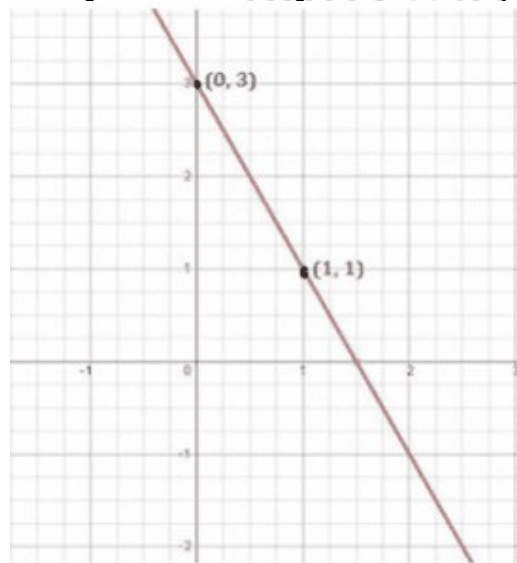
$$3 = 2 + y$$

$$y = 3 - 2$$

$$y = 1$$

x	y
0	3
1	1

The points to be plotted are (0, 3) and (1, 1)



2. Give the equations of two lines passing through (2, 14). How many more such lines are there, and why?

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Solution:

We know that an infinite number of lines pass through a point.

The equation of 2 lines passing through (2,14) should be in such a way that it satisfies the point.

Let the equation be $7x = y$

$$7x - y = 0$$

When $x = 2$ and $y = 14$

$$(7 \times 2) - 14 = 0$$

$$14 - 14 = 0$$

$$0 = 0$$

L.H.S. = R.H.S.

Let another equation be $4x = y - 6$

$$4x - y + 6 = 0$$

When $x = 2$ and $y = 14$

$$(4 \times 2) - 14 + 6 = 0$$

$$8 - 14 + 6 = 0$$

$$0 = 0$$

L.H.S. = R.H.S.

Since both the equations satisfy the point (2,14), then we can say that the equations of two lines passing through (2, 14) are $7x = y$ and $4x = y - 6$

We know that an infinite number of line passes through one specific point.

Since there is only one point (2,14) here, there can be infinite lines that pass through the point.

3. If the point (3, 4) lies on the graph of the equation $3y = ax + 7$, find the value of a.

Solution:

The given equation is

$$3y = ax + 7$$

According to the question, $x = 3$ and $y = 4$

Now, substituting the values of x and y in the equation $3y = ax + 7$,

We get,

$$(3 \times 4) = (a \times 3) + 7$$

$$\Rightarrow 12 = 3a + 7$$

$$\Rightarrow 3a = 12 - 7$$

$$\Rightarrow 3a = 5$$

$$\Rightarrow a = 5/3$$

LOYAL EDUCATION MATHEMATICS

Result Oriented

(NCERT SOLUTION)

[CLASS IX]

The value of a , if the point $(3,4)$ lies on the graph of the equation $3y = ax+7$ is $5/3$.

4. The taxi fare in a city is as follows: For the first kilometre, the fare is ₹8, and for the subsequent distance, it is ₹5 per km. Taking the distance covered as x km and total fare as ₹ y , write a linear equation for this information, and draw its graph.

Solution:

Given,

Total distance covered = x

Total fare = y

Fare for the first kilometre = 8 per km

Fare after the first 1km = 5 per km

If x is the total distance, then the distance after one km = $(x-1)$ km

i.e., fare after the first km = $5(x-1)$

According to the question,

The total fare = Fare of first km + fare after the first km

$$y = 8 + 5(x-1)$$

$$y = 8 + 5(x-1)$$

$$y = 8 + 5x - 5$$

$$y = 5x + 3$$

Solving the equation,

When $x = 0$,

$$y = 5x + 3$$

$$y = 5 \times 0 + 3$$

$$y = 3$$

When $y = 0$,

$$y = 5x + 3$$

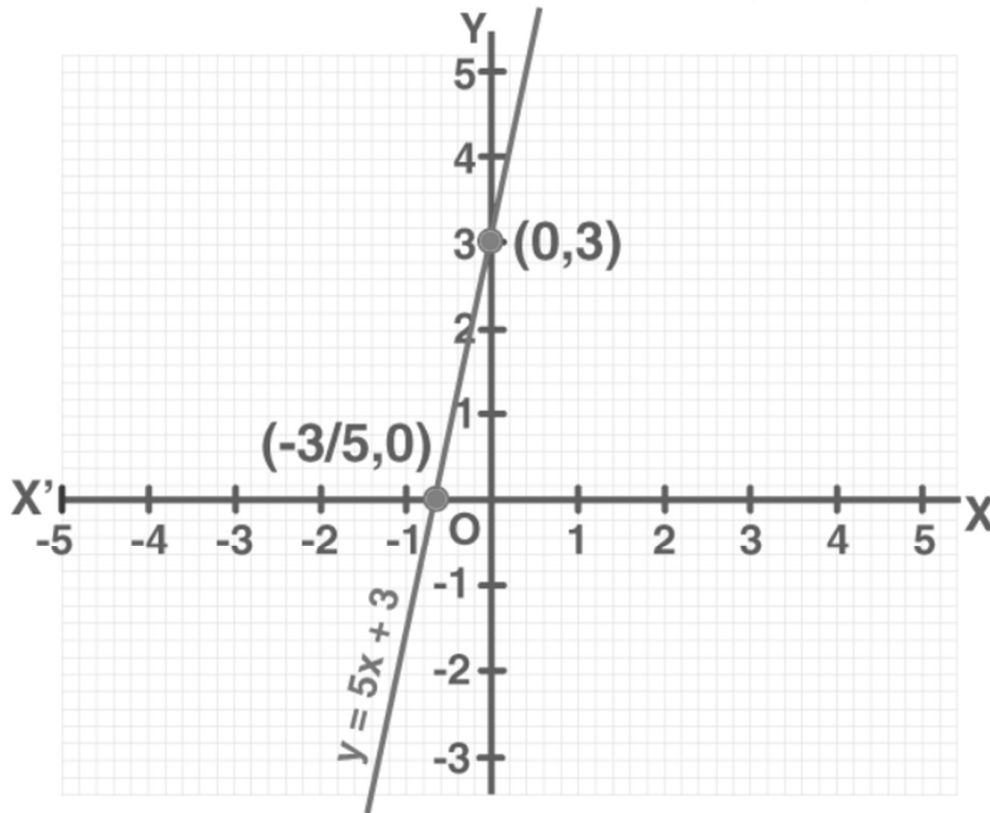
$$0 = 5x + 3$$

$$5x = -3$$

$$x = -3/5$$

x	y
0	3
-3/5	0

The points to be plotted are $(0, 3)$ and $(-3/5, 0)$

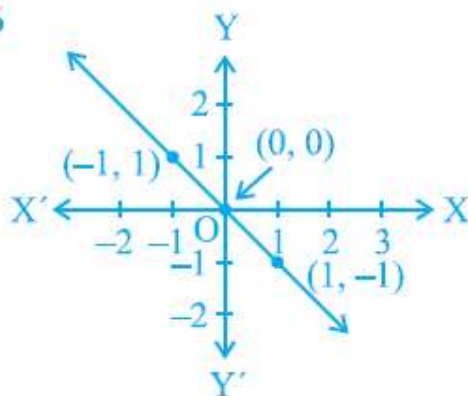


5. From the choices given below, choose the equation whose graphs are given in Fig. 4.6 and Fig. 4.7.

For Fig. 4. 6

- (i) $y = x$
- (ii) $x + y = 0$
- (iii) $y = 2x$
- (iv) $2 + 3y = 7x$

Fig. 4.6



Solution:

The points given in figure 4.6 are $(0,0)$, $(-1,1)$, $(1,-1)$

Substituting the values for x and y from these points in the equations, we get,

(i) $y = x$

$(0,0) \Rightarrow 0 = 0$

$(-1, 1) \Rightarrow -1 \neq 1$ ————— equation not satisfied

$(1, -1) \Rightarrow 1 \neq -1$ ————— equation not satisfied

(ii) $x+y = 0$

$(0,0) \Rightarrow 0+0 = 0$

$(-1, 1) \Rightarrow -1+1 = 0$

$(1, -1) \Rightarrow 1+(-1) = 0$

(iii) $y = 2x$

$(0,0) \Rightarrow 0 = 2 \times 0$

$0 = 0$

$(-1, 1) \Rightarrow 1 = 2 \times (-1)$

$1 \neq -2$ ————— equation not satisfied

$(1, -1) \Rightarrow -1 = 2 \times 1$

$-1 \neq 2$ ————— equation not satisfied

(iv) $2+3y = 7x$

$(0,0) \Rightarrow 2+(3 \times 0) = 7 \times 0$

$2 \neq 0$ ————— equation not satisfied

$(-1, 1) \Rightarrow 2+(3 \times 1) = 7 \times -1$

$5 \neq -7$ ————— equation not satisfied

$(1, -1) \Rightarrow 2+(3 \times -1) = 7 \times 1$

$-1 \neq 7$ ————— equation not satisfied

Since only equation $x+y = 0$ satisfies all the points, the equation whose graphs are given in Fig. 4.6 is

$x+y = 0$

For Fig. 4. 7

(i) $y = x+2$

(ii) $y = x-2$

(iii) $y = -x+2$

(iv) $x+2y = 6$

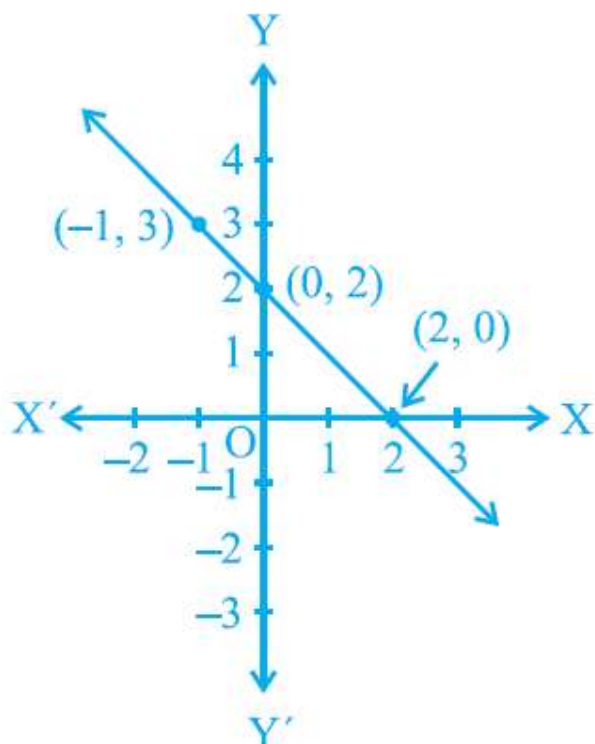


Fig. 4.7

Solution:

The points given in figure 4.7 are $(0,2)$, $(2,0)$, $(-1,3)$

Substituting the values for x and y from these points in the equations, we get,

(i) $y = x + 2$

$(0,2) \Rightarrow 2 = 0 + 2$

$2 = 2$

$(2,0) \Rightarrow 0 = 2 + 2$

$0 \neq 4$ ————— equation not satisfied

$(-1,3) \Rightarrow 3 = -1 + 2$

$3 \neq 1$ ————— equation not satisfied

(ii) $y = x - 2$

$(0,2) \Rightarrow 2 = 0 - 2$

$2 \neq -2$ ————— equation not satisfied

$(2,0) \Rightarrow 0 = 2 - 2$

$0 = 0$

$(-1,3) \Rightarrow 3 = -1 - 2$

$3 \neq -3$ ————— equation not satisfied

$$(iii) y = -x + 2$$

$$(0, 2) \Rightarrow 2 = -0 + 2$$

$$2 = 2$$

$$(2, 0) \Rightarrow 0 = -2 + 2$$

$$0 = 0$$

$$(-1, 3) \Rightarrow 3 = -(-1) + 2$$

$$3 = 3$$

$$(iv) x + 2y = 6$$

$$(0, 2) \Rightarrow 0 + (2 \times 2) = 6$$

$$4 \neq 6 \text{ ————— equation not satisfied}$$

$$(2, 0) \Rightarrow 2 + (2 \times 0) = 6$$

$$2 \neq 6 \text{ ————— equation not satisfied}$$

$$(-1, 3) \Rightarrow -1 + (2 \times 3) = 6$$

$$5 \neq 6 \text{ ————— equation not satisfied}$$

Since only equation $y = -x + 2$ satisfies all the points, the equation whose graphs are given in Fig. 4.7 is

$$y = -x + 2$$

6. If the work done by a body on application of a constant force is directly proportional to the distance travelled by the body, express this in the form of an equation in two variables and draw the graph of the same by taking the constant force as 5 units. Also, read from the graph the work done when the distance travelled by the body is

(i) 2 units

(ii) 0 unit

Solution:

Let the distance travelled by the body be x and the force applied on the body be y .

It is given that,

The work done by a body is directly proportional to the distance travelled by the body.

According to the question,

$$y \propto x$$

$$y = 5x \text{ (5 is a constant of proportionality)}$$

Solving the equation,

(i) when $x = 2$ units,

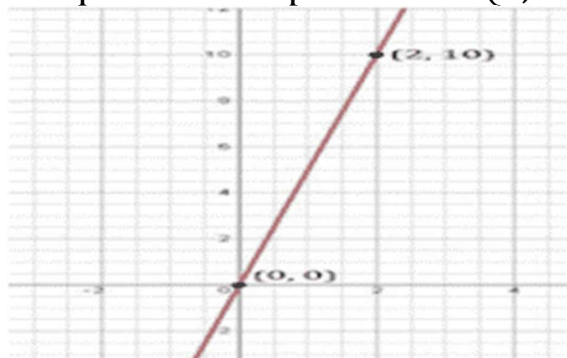
$$\text{then } y = 5 \times 2 = 10 \text{ units}$$

$$(2, 10)$$

(ii) when $x = 0$ units,
then $y = 5 \times 0 = 0$ units.

$(0, 0)$

The points to be plotted are $(2, 10)$ and $(0, 0)$



7. Yamini and Fatima, two students of Class IX of a school, together contributed ₹ 100 towards the Prime Minister's Relief Fund to help the earthquake victims. Write a linear equation which satisfies this data (You may take their contributions as ₹ x and ₹ y). Draw the graph of the same.

Solution:

Let Yamini's donation be ₹ x and Fatima's donation be ₹ y

According to the question,

$$x + y = 100$$

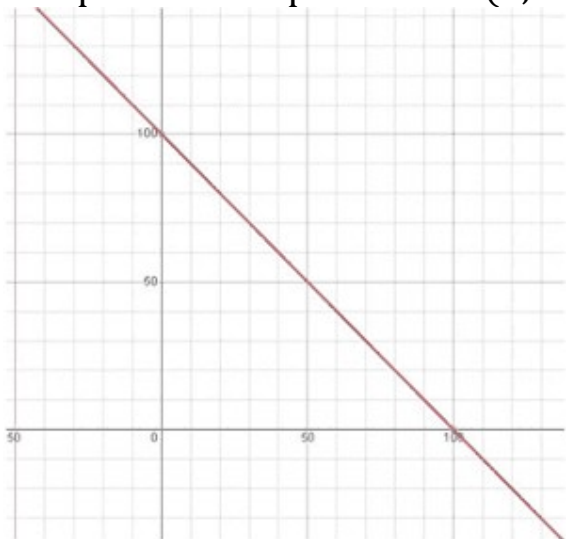
We know that,

when $x = 0$, $y = 100$

when $x = 50$, $y = 50$

when $x = 100$, $y = 0$

The points to be plotted are $(0, 100)$, $(50, 50)$, $(100, 0)$



8. In countries like USA and Canada, the temperature is measured in Fahrenheit, whereas in countries like India, it is measured in Celsius. Here is a linear equation that converts Fahrenheit to Celsius:

$$F = \left(\frac{9}{5}\right)C + 32$$

(i) Draw the graph of the linear equation above using Celsius for the x-axis and Fahrenheit for the y-axis.

(ii) If the temperature is 30°C, what is the temperature in Fahrenheit?

(iii) If the temperature is 95°F, what is the temperature in Celsius?

(iv) If the temperature is 0°C, what is the temperature in Fahrenheit, and if the temperature is 0°F, what is the temperature in Celsius?

(v) Is there a temperature which is numerically the same in both Fahrenheit and Celsius? If yes, find it.

Solution:

(i) According to the question,

$$F = (9/5)C + 32$$

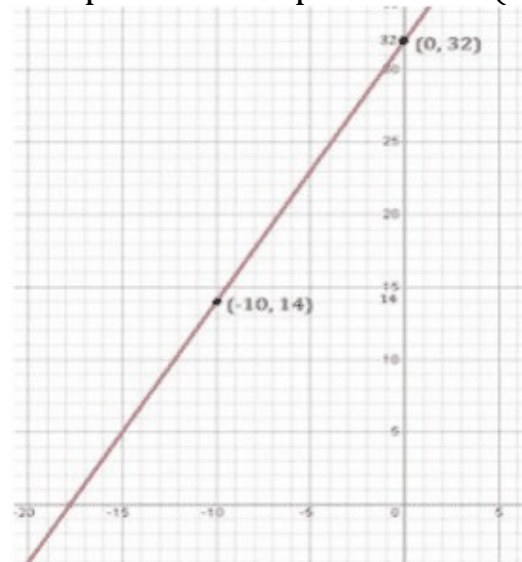
Solving the equation,

We get,

$$\text{When } C = 0, F = 32$$

$$\text{When } C = -10, F = 14$$

The points to be plotted are (0, 32), (-10, 14)



(ii) When $C = 30$,

$$F = (9/5)C + 32$$

$$F = (9 \times 30)/5 + 32$$

$$= (9 \times 6) + 32$$

$$= 54 + 32$$

$$= 86^\circ\text{F}$$

(iii) When $F = 95$,

$$95 = (9/5)C + 32$$

$$(9/5)C = 95 - 32$$

$$(9/5)C = 63$$

$$C = (63 \times 5)/9$$

$$= 35^\circ\text{C}$$

(iv) When $C = 0$,

$$F = (9/5)C + 32$$

$$F = (9 \times 0)/5 + 32$$

$$= 0 + 32$$

$$= 32^\circ\text{F}$$

When $F = 0$,

$$0 = (9/5)C + 32$$

$$(9/5)C = 0 - 32$$

$$(9/5)C = -32$$

$$C = (-32 \times 5)/9$$

$$= -17.7777$$

$$= -17.8^\circ\text{C}$$

(v) When $F = C$,

$$C = (9/5)C + 32$$

$$C - (9/5)C = 32$$

$$(5-9)C/5 = 32$$

$$(-4/5)C = 32$$

$$(-4/5)C = (-32 \times 5)/4$$

$$= -40^\circ\text{C}$$

Hence, -40° is the temperature which is numerically the same in both Fahrenheit and Celsius.

Exercise 4.4 Page: 77

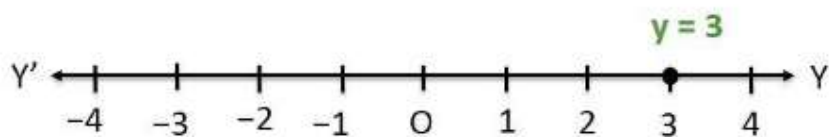
1. Give the geometric representations of $y = 3$ as an equation

(i) in one variable

(ii) in two variables

Solution:

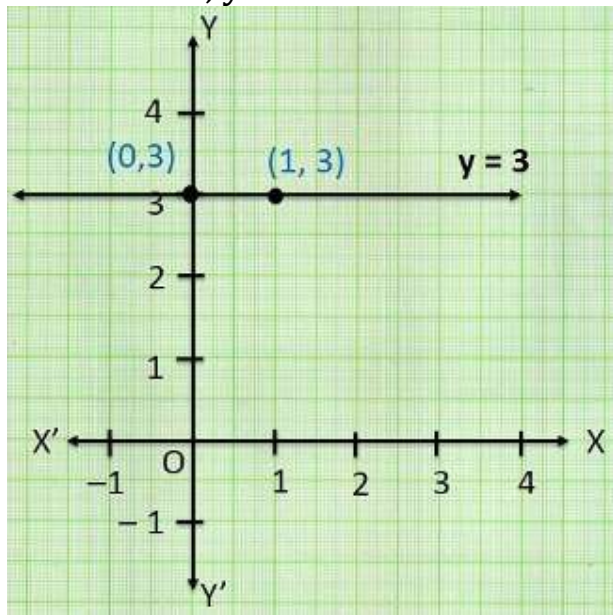
1. In one variable, $y = 3$



(ii) In two variables, $0x + y = 3$

When $x = 0$, $y = 3$

When $x = 1$, $y = 3$



2. Give the geometric representations of $2x + 9 = 0$ as an equation

(i) in one variable

(ii) in two variables

Solution:

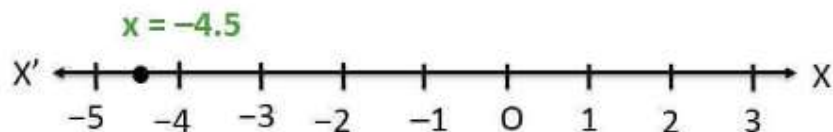
(i) In one variable,

$$2x + 9 = 0$$

$$2x = -9$$

$$x = -9/2$$

$$x = -4.5$$



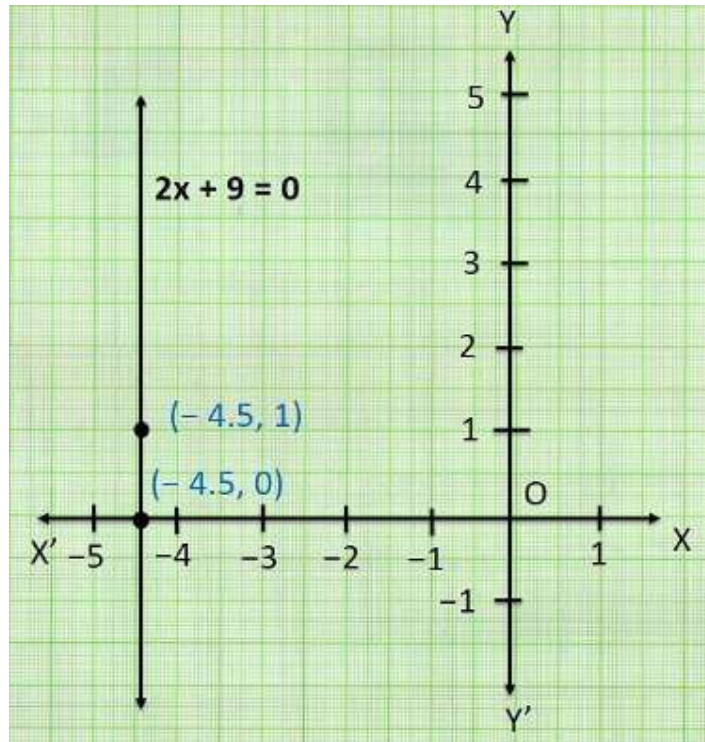
(ii) In two variables,

$$2x + 9 = 0$$

$$2x + 0y + 9 = 0$$

When $y = 0$, $x = -4.5$

When $y = 1$, $x = -4.5$



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